**Proceedings of the 2018 Design of Medical Devices Conference**

**DMD2018**

**April 9-12, 2018, Minneapolis, MN, USA**

DMD2018-6862

**Real-Time, Non-Contacting Position Tracking of Medical Devices and Surgical Tools through the Analysis of Magnetic Field Vectors**

|  |  |
| --- | --- |
| Mohammad Odeh  Institute for Simulation and Training, University of Central Florida  Orlando, Florida, USA | Edward Daniel Nichols  Institute for Simulation and Training, University of Central Florida  Orlando, Florida, USA |

|  |  |
| --- | --- |
| Fluvio L Lobo Fenoglietto  Institute for Simulation and Training, University of Central Florida  Orlando, Florida, USA | Jack Stubbs  Institute for Simulation and Training, University of Central Florida  Orlando, Florida, USA |

# Background

The adoption of robotically assisted surgeries has increased due to the reduction in patient recovery times. To highlight just how quickly this technology has gained prevalence, Beasley writes the *Da Vinci* “was used in 80% of radical prostatectomies performed in the U.S. for 2008, just nine years after the system went on the market” [8]. The *Da Vinci* is not alone. Competition in the field is increasing, driving the development of more versatile, more cost-effective and more autonomous systems. However, robotic systems carry the inherent technical requirement for accurate, on-demand spatial information about their environments. For example, Renishaw’s *neuromate* and Accuray’s *CyberKnife* both require the precise location of fiducial markers **[REFS]**. [Others, like Cambridge Medical Robotics’ Versius and Medrobotics’ *Flex* operators rely upon active imaging or access to direct line of sight **[REFS]**.

Hence, as such systems continue to technically advance across a broad scope, that inherent technical requirement for spatial awareness data will only increase. Machine-learning algorithms driving the interconnected array of robotic surgical assistants envisioned by Verb Surgical would need data for processing **[REFS]**; surgeons performing teleoperations across oceans would benefit from the availability of high-quality, real-time, auxiliary sensor information that enables extension of their dexterity and spatial awareness beyond what might be provided for by a robotic platform alone. Furthermore, especially as such technologies proliferate, providers would desire easily deployable, low-profile, cost-effective user input systems for simulation programs designed to train aspiring and established healthcare professionals on using state-of-the-art medical tools.

To advance this field and to fulfill an imperative to provide simulation inputs for our own training applications, we have set out to construct a robust, scalable, highly-customizable, and non-intrusive system for dynamically tracking point objects in a volumetric space. Given that human tissues are permeable to magnetic flux, magnetic fields are well-characterized, and there exists a wide variety of open-sourced hardware, our system achieves this by precisely and dynamically locating an arbitrary magnetic field source, such as any permanent magnet, in a volumetric space within the range of our array. Ultimately, this extremely low-cost proof-of-concept prototype serves as a foundation for exploring this approach in the medical industry.

# Methods

**Analytical Foundation**

Electromagnetic fields are characterized by fundamental principles. Given a classic magnetic dipole centered at the origin, its magnetic induction can be expressed as:

|  |  |
| --- | --- |
|  | (1) |

Whereby the relationship is dependent on the orientation and strength of its magnetic moment vector, given by, as well as the location of the arbitrary point of interest with respect to the center of the magnet, represented by vector. Equation (1) can be modified to express the strength of the magnetic field **,** which is what an observing magnetometer normal to the level surface of the magnetic field would perceive; which may further be broken into a more convenient polar component form, given the intrinsic rotational symmetry of isofield lines about . Based on the work of Chen *et al* [5], expressing the location of the center of a magnet with respect to the magnetic field vectors observed by three sensors in predefined relative positions fully satisfies a system of equations when the magnet is in a fixed North pole orientation along the system’s internally defined x-axis:

|  |  |
| --- | --- |
|  | (2) |
|  | (3) |
|  | (4) |

Whereby, represents a sensor in the array, is the distance to the center of the magnet for the sensor, is the relative offset from a designated origin with respect to the sensor, represents the angle made by the north pole of the magnet and the radial component of, and K represents a constant that encompasses the magnitude of the dipole moment, magnetic permeability of free space, and the relative permeability of the magnet’s own material.

However, one must maintain certain minimum conditions for a solution to converge numerically:

1. An origin must be defined with respect to the relative fixed positions and orientations of the sensors.
2. The constant value of the magnetic field strength coefficient K of an arbitrary magnet has been closely approximated or is otherwise known.
3. A constant magnetic field source of perceivable threshold exists within the optimal range of at least three sensors in the sensor array.

In addition, to refine accuracy, certain physical restrictions facilitate these conditions:

1. Ambient magnetic fields must be mitigated; or their noise must be otherwise overcome.
2. The magnet’s form factor is minimized to yield closer adherence to presupposed principles.

To begin achieving these conditions, we designated the sensor in the bottom left corner of our sensor array (Figure 1) to be the origin. All sensors’ axis in the array are aligned with each other.

**Magnet Selection**

In accordance with our design prerogative, permanent magnets were chosen to enable a simple but versatile system that can deliver precision without compromising costs. Permanent magnets are readily available in different shapes, sizes and strength. Therefore, surgical tools or medical devices can be equipped with an appropriate magnet that demands only minimal design changes, if any at all. Permanent magnets also do not require power, which further reduces the need for the redesign and adaptation of the tool or device to be tracked.

A disc-shaped, 30 mm in diameter permanent magnet was found to comply with our simulation application’s low-modification parameter, so it was chosen to test and evaluate our proof-of-concept system. The magnet’s dipole field was assumed to be ideal and its diploe moment was calculated empirically.

**Empirical Approximation of K for Arbitrary Magnet**

Our team devised an empirical approach to approximate the value of K using a single *SparkFun LSM9DS1 IMU* and a custom CNC machine. The CNC was used to move a fitted permanent magnet precisely along the axis, thus simplifying Eqns. (2), (3) and (4) into Equation (5).

|  |  |
| --- | --- |
|  | (5) |

The procedure employed for the approximation of K, for each magnet, can be summarized in the following six steps:

1. The magnet was placed at 50mm away from the IMU sensor such that it reads.
2. A sample value for was obtained andan accurate approximation for K was computed using Eqn. (5).
3. The magnet was moved by mm to  
   ().
4. Another sample of K was approximated from a new sample of.
5. Steps 3 and 4 were repeated up to =75mm, recording the values of , and K each time.
6. An approximated result of K was yielded from averaging the sampled points.

It was observed that the calculated value of K varies along the different positions. The rigorous characterization of these variations and their impact on the system was left as future work. However, it was also found to be possible to continuously improve the accuracy of the approximated value of K for a magnet by minimizing the and components of the magnetic field readings driven by the magnet during the procedure.

While , the approximated K yielded physically reasonable position solutions. Nevertheless, the marginal gain in accuracy using a more rigorous method was not significantly beneficial to our purpose and the team opted to use the protocol defined earlier to approximate the value of K for any future work.

**Sensor Array and Tracking Algorithm**

To determine the position of the permanent magnet in 3D space, at least three magnetic field measurements are needed. In other words, three sensors are needed to triangulate the position of the permanent magnet. To enhance the range and accuracy of the tracking system however, an array of six *SparkFun LSM9DS1 IMU* sensors was built. Due to I2C address conflicts, magnetometer communication was mediated using a *SparkFun 74HC4051 8-channel* *multiplexer*. Data was driven through an Arduino-compatible microcontroller such as the *Arduino Mega 2560* or *PJRC’s Teensy 3.2* (Figure #). Microcontrollers formatted and transmitted magnetometer data through a Serial Bus to a PC running a custom Python script. The entire set-up was mounted between two aluminum breadboard with M6 taps every 25 mm. 3D-printed holders were fabricated to secure the magnetometers and permanent magnets.

Sensor readings were taken by the magnetometers at 80Hz, yielding the XYZ components of with respect to the sensor orientation. Geomagnetism was partially accounted for using the board’s built-in declination adjustment function. To mitigate the effect of ambient magnetic fields, sensor readings were averaged over 50 samples. The resultant, treated as an offset, was then subtracted from later readings. Readings ranged between ±20 Milligauss and ±16 Gauss, in accordance to the built-in 16-bit analog to digital converter in the chip.

Data retrieval and position tracking was driven by a custom Python script developed on a PC. Based on Eqns. (2), (3) and (4), each magnetometer allowed the Python script to assemble one equation, for a total of six equations using the entire array. The resulting non-linear system was solved numerically. SciPy’s implementation of the Levenberg-Marquardt (LMA) method was used to solve the resulting non-linear system. The script constructed a determinable system of equations using the data from the three magnetometers observing the largest. LMA was chosen for its robustness and speed of convergence. Solutions typically converge within 2 milliseconds. SciPy’s LMA combines Newton-Raphson’s algorithm and the Steepest Descent method to converge even in the case of a poor initial guess. However, like any numerical method, effective convergence still relies on the initial guess’ proximity to the solution. To overcome this issue, the centroid of the triangle described by the three magnetometers with the largest readings was used as the initial guess.

Upon convergence of the LMA, values were logged to determine point accuracy (Table 1) and motion tracking capabilities (Figure #, #). The entire process described above, from sensor calibration to data collection and numerical solution has been summarized in Figure 2.

# Results

**Approximation of K**

Following the CNC-based approximation protocol described earlier, the magnitude of the magnetic field moment for the 30 mm permanent magnet was found to be.

**Position Tracking Accuracy**

Position tracking accuracy was studied by placing the permanent magnet at 20 different locations over the sensor array, varying x, y and z coordinates using 3D-printed standoffs. At each location, sensor readings and position calculations were recorded over 20 seconds. Accuracy was defined as the difference between the expected and observed x, y and z coordinates (∆x, ∆y, ∆z). A percentage error was calculated as the ratio of these differences to the original X and Y positions. The values reported here represent the average position difference and error among the 20 points sampled using each magnet (Table 2, 3).

**Motion Tracking**

In addition to static position accuracy, the system was tested for motion tracking. A 3D-printed track was designed to guide the permanent magnet on a constrained path as its position was approximated by the sensor array. Position in 3D space (x, y, and z coordinates of the magnet) was time-stamped and recorded by the sensor array. Scatter plot were generated for each run (Figure #). To maintain the magnet on the track, a carriage was 3D-printed to hold the magnet. The carriage, in turn, generated a constant offset in the z coordinate of the magnet (Figure #, #).

The motion tracking performance of the system was determined by estimating a sampling rate. For eight trials, position measurements were recorded for the duration of one lap around the track. The number of measurements recorded was divided by the lap time to estimate a sampling rate of 23.50 ± 0.0404 samples/sec (N=8).

INterpretation and future work

The most significant accomplishments of the work presented here encompass the design and implementation of a non-contacting position tracking method and system using affordable, open-source hardware and software components. The system gave accurate position results and performed over a wider range than other similar applications [2, 5, and 6]. The system also sustained an almost constant sampling rate when tracking a moving magnet. Last but not least, our method worked with off-the-shelf permanent magnets. This capability allows for easy adaptation to devices or applications where after-market modifications must be kept to a minimum.

Throughout the development of our system, our team encountered some limitations which had an effect on the results presented here.First, the system and methodology must be refined to account for rotations of the permanent magnet. This may require the integration of rotation calculations as described by Chen et al. [5]. Second, the full 3D tracking range of the sensor array must be studied thoroughly. Initial results in 2D and 3D tracking revealed areas and volumes where position accuracy is inconsistent with the results presented here. Understanding range limitations may require automated, accurate testing equipment. CNC systems can be programmed to pursue a path and, therefore, perform an extensive position accuracy test and identify range limits. The same level of automation can be used to more objectively determine the system’s performance during motion tracking.

Future work will seek to mitigate limitations by improving the data collection and position calculation algorithms. As development moves forward, automated mechanisms will be implemented to evaluate system performance. Finally, hardware improvements will be aimed toward reducing system footprint by implementing micro-computers like the *Raspberry Pi 3*.

References

[1] Han, X., Seki, H., Kamiya, Y., and Hikizu, M. “Wearable handwriting input device using magnetic field Geomagnetism cancellation in position calculation.” *Precision Engineering* Vol. 33 Issue 1 (2009), pp: 37-43. DOI 10.1016/j.precisioneng.2008.03.008.

[2] Han, X., Seki, H., Kamiya, Y., and Hikizu, M. “Wearable handwriting input device using magnetic field 2nd report: Influence of misalignment of magnet and writing plane.” *Precision Engineering* Vol. 34 Issue 3 (2010), pp: 425-430. DOI 10.1016/j.precisioneng.2009.12.005

[3] Raab, F., Blood, E., Steiner, T., and Jones, H. “Magnetic Position and Orientation Tracking System” *IEEE Transactions on Aerospace and Electronic Systems* Vol. AES-15 No. 5 (1979), pp: 709-718

[4] Moeslund, T., and Granum, E. “A Survey of Computer Vision-Based Human Motion Capture.” *Computer Vision and Image Understanding* Vol. 81, Issue 3 (2001), pp: 231-268. DOI 10.1006/cviu.2000.0897

[5] Chen, K., Lyons, K., White, S., and Patel, S. “uTrack: 3D Input Using Two Magnetic Sensors” In *Proceedings of the 26th Annual ACM Symposium on User Interface Software and Technology (UIST 2013).* pp: 237-244. St. Andrews, UK, October 8th-11th, 2013. DOI 10.1145/2501988.2502035

[6] Chen, K., Patel, S., and Keller, S. “Finexus: Tracking Precise Motions of Multiple Fingertips Using Magnetic Sensing” In *Proceedings of the 2016 CHI Conference on Human Factors in Computing Systems (CHI 2016), ACM.* pp: 1504-1514. San Jose, California, USA, May 7th-12th, 2016. DOI 10.1145/2858036.2858125

[7] Yoon, S., Huo, K., and Ramani, K. “TMotion: Embedded 3D Mobile Input using Magnetic Sensing Technique” In *Proceedings of the Tenth International Conference on Tangible, Embedded, and Embodied Interaction (TEI 2016), ACM.* pp: 21-29. Eindhoven, Netherlands, February 14th-17th, 2016. DOI 10.1145/2839462.2839463

[8] Beasley, R. A.: “Medical Robots: Current Systems and Research Directions” In *Hindawi Journal of Robotics Volume 2012, Article ID 401613*. DOI 10.1155/2012/401613